

## Types of Triangles – Classify by SIDES

Circle the correct name(s) of the triangle below:

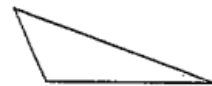
$\triangle A$   $\triangle B$   $\triangle C$   $\triangle ABC$   $\triangle CBA$   $\triangle ACB$



### SCALENE $\triangle$

How many  $\cong$  sides does a scalene  $\triangle$  have? *none*

Mark the sides of the triangle  
To show that NONE are the same  $\rightarrow$



### EQUILATERAL $\triangle$

How many  $\cong$  sides **must** an equilateral  $\triangle$  have? *3*

Can it have more than that amount? *no*

Can it have less than that amount?

*no*

Mark the  $\cong$  sides in the triangle  $\rightarrow$



### ISOSCELES $\triangle$

How many  $\cong$  sides **must** an isosceles  $\triangle$  have?

Can it have more than that amount? *at least 2*

Can it have less than that amount? *yes*

Can it have less than that amount?

*no*

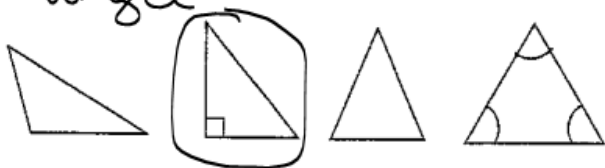
Mark the  $\cong$  sides in the triangle  $\rightarrow$



## Types of Triangles – Classify by ANGLES

\* *one right angle*

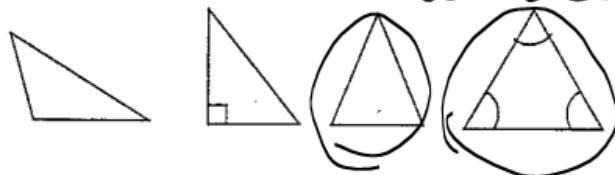
### RIGHT $\triangle$



Circle the RIGHT  $\triangle$  (there may be more than one)

### ACUTE $\triangle$

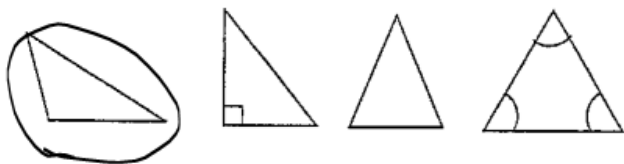
*all 3  $\angle$ s are acute*



Circle the ACUTE  $\triangle$  (there may be more than one)

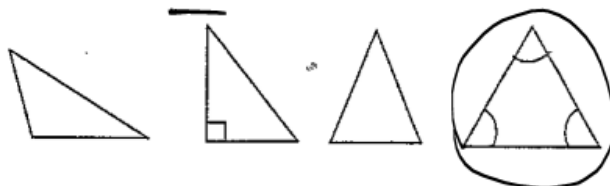
\* *one  $\angle$  is obtuse*

### OBTUSE $\triangle$



Circle the OBTUSE  $\triangle$  (there may be more than one)

### EQUIANGULAR $\triangle$



Circle the EQUIANGULAR  $\triangle$  (there may be more than one)

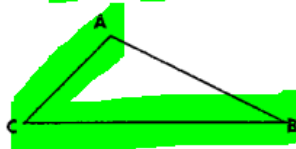
## PARTS OF A TRIANGLE

\*  $\angle$  btwn  
given sides

**INCLUDED ANGLE**

What is the included angle for  $\overline{AC}$  and  $\overline{BC}$ ?

$\angle A$   $\angle B$   $\angle C$

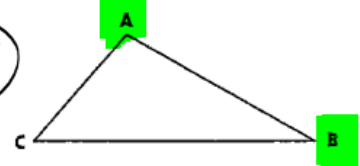


\* Side btwn  
given  $\angle$ s

**INCLUDED SIDE**

What is the included side for  $\angle A$  and  $\angle B$ ?

$\overline{AC}$   $\overline{CB}$   $\overline{AB}$

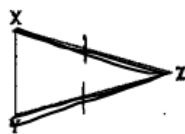


\*  $\cong$  Sides of  
isos  $\Delta$

**LEGS**

\* Sides adj  
to the  $\angle$

Identify the legs in each of the triangles below



$\overline{XY}$   $\overline{YZ}$   $\overline{XZ}$

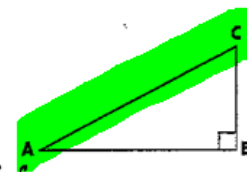


$\overline{AC}$   $\overline{CB}$   $\overline{AB}$

**HYPOTENUSE**

What is the hypotenuse for  $\Delta ABC$ ?

$\overline{AC}$   $\overline{CB}$   $\overline{AB}$



\* Side across  
the  $\angle$

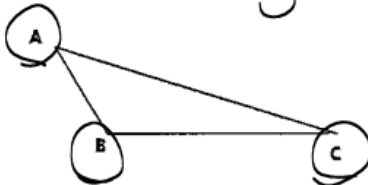
**VERTEX of a triangle**

How many vertices are there in any triangle?

3

What are the vertices of  
this triangle?

A, B, C

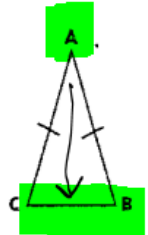


**VERTEX ANGLE in an isosceles  $\Delta$  (p.236)**

What is the vertex angle in this triangle?

$\angle A$   $\angle B$   $\angle C$

\*  $\angle$  btwn  $\cong$   
sides

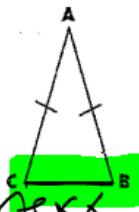


**BASE in an isosceles  $\Delta$**

What is the base in this triangle?

$\overline{AC}$   $\overline{CB}$   $\overline{AB}$

\* Side across from vertex  $\angle$

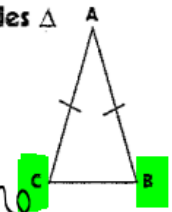


**BASE ANGLES in an isosceles  $\Delta$**

What are the base angles in this triangle?

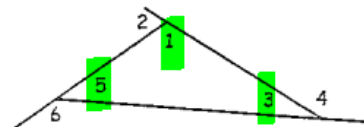
$\angle A$   $\angle B$   $\angle C$

\* Angles adj to the  
base



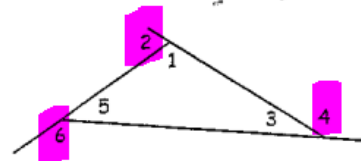
**INTERIOR  $\angle$  of a  $\Delta$**

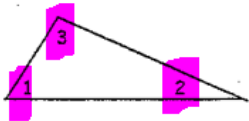
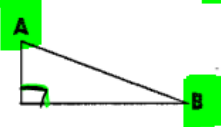
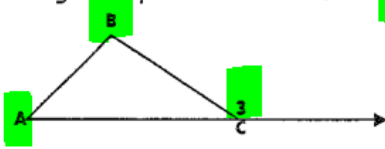
Circle the interior angles in the picture below.



**EXTERIOR  $\angle$  of a  $\Delta$**

Circle the exterior angles in the picture below.



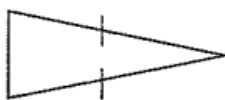
TRIANGLE THEOREMS	
<p><b>Define "corollary":</b> a statement that can be proven by using the theorem</p>	
<p><b><u>Sum Theorem:</u></b></p> <p>The sum of the interior angles in a triangle is <math>180^\circ</math></p>  <p><math>m\angle 1 + m\angle 2 + m\angle 3 = 180^\circ</math></p>	<p><b><u>Corollary to Sum Theorem:</u></b></p> <p>The acute angles in a RIGHT <math>\Delta</math> are complementary</p>  <p><math>\angle A</math> and <math>\angle B</math> are complementary</p>
<p><b><u>Exterior <math>\angle</math> Theorem:</u></b></p> <p>The measure of the exterior <math>\angle</math> of a triangle is equal to the sum of the 2 non-adjacent interior <math>\angle</math>'s</p>  <p><math>m\angle A + m\angle B = m\angle 3</math></p>	

## PRACTICE PROBLEMS (All answers are on the bottom of page 23)

### 1. CLASSIFYING TRIANGLES -

Use the definitions and pictures on **page 20** to classify the triangles by their **SIDES** and **ANGLES**.

a.)



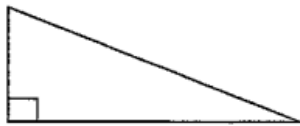
By sides...

isosceles equilateral scalene

By angles...

right acute obtuse equiangular

b.)



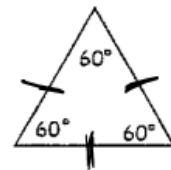
By sides...

isosceles equilateral scalene

By angles...

right acute obtuse equiangular

c.)



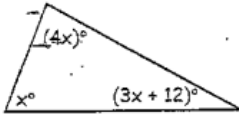
By sides...

isosceles equilateral scalene

By angles...

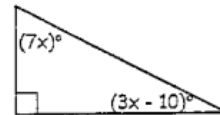
right acute obtuse equiangular

2.



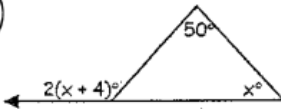
$$\begin{aligned}
 x + 4x + 3x + 12 &= 180 \\
 8x + 12 &= 180 \\
 8x &= 168 \\
 x &= 21
 \end{aligned}$$

3.



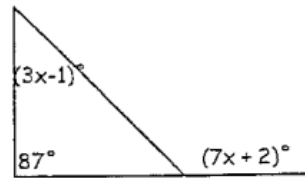
$$\begin{aligned}
 7x + 3x - 10 &= 90 \text{ or} \\
 7x + 3x - 10 + 90 &= 180 \\
 x &= 10
 \end{aligned}$$

4.



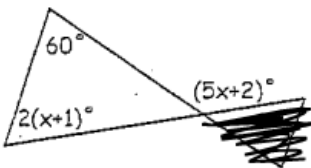
$$\begin{aligned}
 50 + x &= 2x + 8 \\
 50 &= x + 8 \\
 x &= 42
 \end{aligned}$$

5.



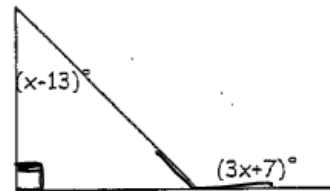
$$\begin{aligned}
 3x - 1 + 87 &= 7x + 2 \\
 x &= 21
 \end{aligned}$$

6.



$$\begin{aligned}
 60 + 2x + 2 &= 5x + 2 \\
 x &= 20
 \end{aligned}$$

7.



$$\begin{aligned}
 x - 13 + 90 &= 3x + 7 \\
 x &= 35
 \end{aligned}$$